

**NOTES:**

Design problems and some Digital Logic implementation problems can have  $\infty$  solutions. One solution is shown below.

**SOLUTIONS:****Problem 1:**

Cascode amplifier with active load so the gain

$$A_v = -\left(\frac{g_m}{g_0}\right) = -\frac{0.039}{10 \mu} = -3900 \text{ V/V}$$

$$g_m = \frac{I_{CQ}}{V_t} = \frac{1 \text{ mA}}{25.8 \text{ mV}} = 0.039 \text{ \& } g_0 = \frac{1 \text{ mA}}{100 \text{ V}} = 10 \mu$$

**Problem 2:**

$$A_v = -\frac{g_m^2}{g_0 g_\pi} \frac{1}{2} \cong -196000 \text{ V/V}$$

$$g_m = \frac{I_{CQ}}{V_t} = \frac{1 \text{ mA}}{25.8 \text{ mV}} = 0.039 \text{ \& } g_0 = \frac{1 \text{ mA}}{100 \text{ V}} = 10 \mu \text{ \& } g_\pi = \frac{1 \text{ mA}}{100 * 25.8 \text{ mV}} = 0.388 \text{ m}$$

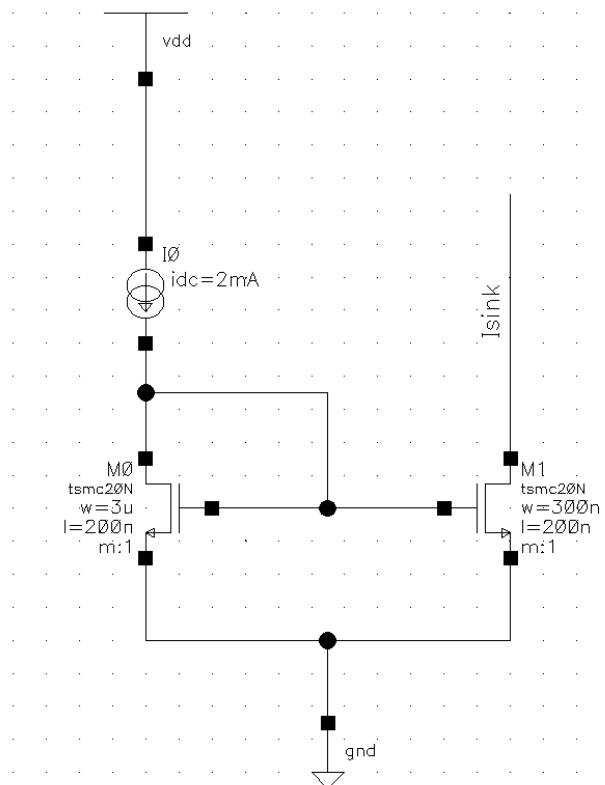
**Problem 3:**

$$2 + A_v V_{in} = 2 + (1 * 10^{-6})(-1.96 * 10^5) = -2.196 \text{ V}$$

This means it would be very difficult to get the system to be biased correctly.

**Problem 4:**

a) Design is shown below, the ratio of W/L of M1 to W/L of M0 is 1:10



b) We need M1 to be in saturation and we know  $I_{DSQ} = 200 \mu A$

$$V_{GS} - V_T = \sqrt{\frac{2 * I_{DSQ}}{\mu C_{ox} * \frac{W}{L}}} = \sqrt{\frac{2 * 200 \mu}{350 \mu * \frac{3}{2}}} = 0.873 V$$

$V_{DS} > V_{GS} - V_T$  therefore  $V_{Drainmin} = 0.873 V$

**Problem 5:**

$$V_{OUT} = 8 - I_{out} * R \rightarrow I_{out} = 50 \mu * \frac{15}{1} * \frac{1}{5} = 150 \mu A$$

$$V_{OUT} = 8 - 150 \mu * 25 k = 4.25 V$$

$$V_{GS} - V_T = \sqrt{\frac{2 * I_{DSQ}}{\mu C_{ox} * \frac{W}{L}}} = \sqrt{\frac{2 * 150 \mu}{350 \mu * \frac{15}{1}}} = 0.239 V \rightarrow \text{Saturation assumption validated}$$

**Problem 6:**

| High |   |     | OR  |   |     | A ~B        |   |     | A   |   |     |
|------|---|-----|-----|---|-----|-------------|---|-----|-----|---|-----|
| A    | B | Out | A   | B | Out | A           | B | Out | A   | B | Out |
| 1    | 1 | 1   | 1   | 1 | 1   | 1           | 1 | 1   | 1   | 1 | 1   |
| 1    | 0 | 1   | 1   | 0 | 1   | 1           | 0 | 1   | 1   | 0 | 1   |
| 0    | 1 | 1   | 0   | 1 | 1   | 0           | 1 | 0   | 0   | 1 | 0   |
| 0    | 0 | 1   | 0   | 0 | 0   | 0           | 0 | 1   | 0   | 0 | 0   |
| ~A B |   |     | B   |   |     | (AB) (~A~B) |   |     | AND |   |     |
| A    | B | Out | A   | B | Out | A           | B | Out | A   | B | Out |
| 1    | 1 | 1   | 1   | 1 | 1   | 1           | 1 | 1   | 1   | 1 | 1   |
| 1    | 0 | 0   | 1   | 0 | 0   | 1           | 0 | 0   | 1   | 0 | 0   |
| 0    | 1 | 1   | 0   | 1 | 1   | 0           | 1 | 0   | 0   | 1 | 0   |
| 0    | 0 | 1   | 0   | 0 | 0   | 0           | 0 | 1   | 0   | 0 | 0   |
| NAND |   |     | XOR |   |     | ~B          |   |     | A~B |   |     |
| A    | B | Out | A   | B | Out | A           | B | Out | A   | B | Out |
| 1    | 1 | 0   | 1   | 1 | 0   | 1           | 1 | 0   | 1   | 1 | 0   |
| 1    | 0 | 1   | 1   | 0 | 1   | 1           | 0 | 1   | 1   | 0 | 1   |
| 0    | 1 | 1   | 0   | 1 | 1   | 0           | 1 | 0   | 0   | 1 | 0   |
| 0    | 0 | 1   | 0   | 0 | 0   | 0           | 0 | 1   | 0   | 0 | 0   |
| ~A   |   |     | ~AB |   |     | NOR         |   |     | Low |   |     |
| A    | B | Out | A   | B | Out | A           | B | Out | A   | B | Out |
| 1    | 1 | 0   | 1   | 1 | 0   | 1           | 1 | 0   | 1   | 1 | 0   |
| 1    | 0 | 0   | 1   | 0 | 0   | 1           | 0 | 0   | 1   | 0 | 0   |
| 0    | 1 | 1   | 0   | 1 | 1   | 0           | 1 | 0   | 0   | 1 | 0   |
| 0    | 0 | 1   | 0   | 0 | 0   | 0           | 0 | 1   | 0   | 0 | 0   |

The named ones are the most commonly used

**Problem 7:**

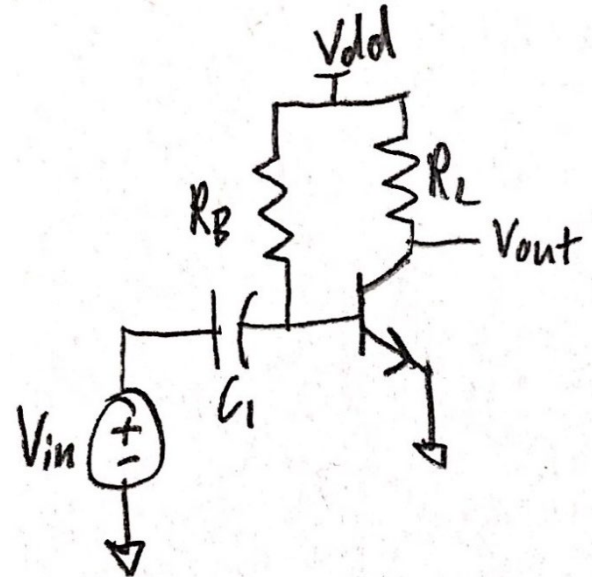
Assume  $C_1$  is large, and set  $V_{DD} = 10V$

$$I_C = \frac{V_{DD} - V_{outQ}}{R_L} = \beta_n I_B = 100 * \frac{V_{DD} - 0.6V}{R_B}$$

$$\frac{10V - 5V}{10k\Omega} = 100 * \frac{10V - 0.6V}{R_B}$$

$$R_B = 1.88 M\Omega$$

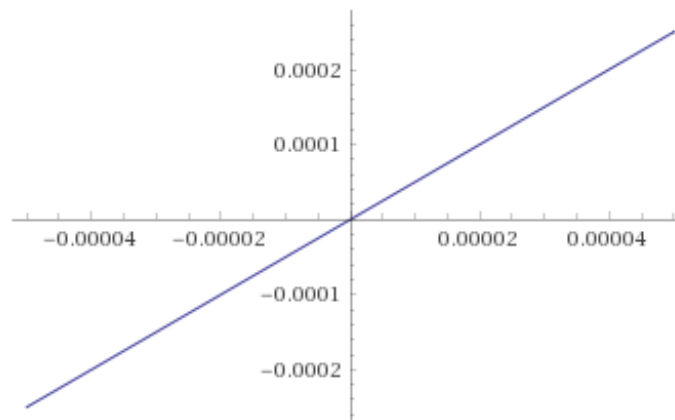
Image of design is on the right.

**Problem 8:**

$$a) I_{out} = \frac{A_{E1}}{A_{E0}} (I_{in} + I_{BS}) - I_{BO} = 5I_{BS} + 250\mu - 250\mu = 5I_{in}$$

b) I used WolframAlpha

Plot:

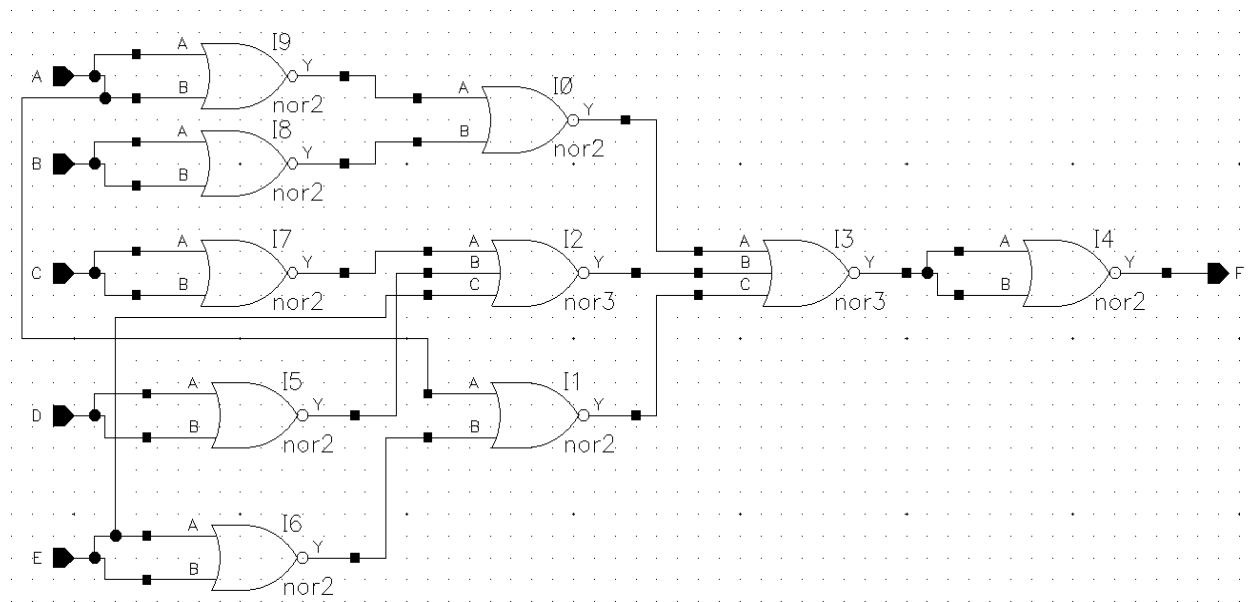


**Problem 9:**

a.)  $F = AB + CDE\bar{E} + \bar{A}E$

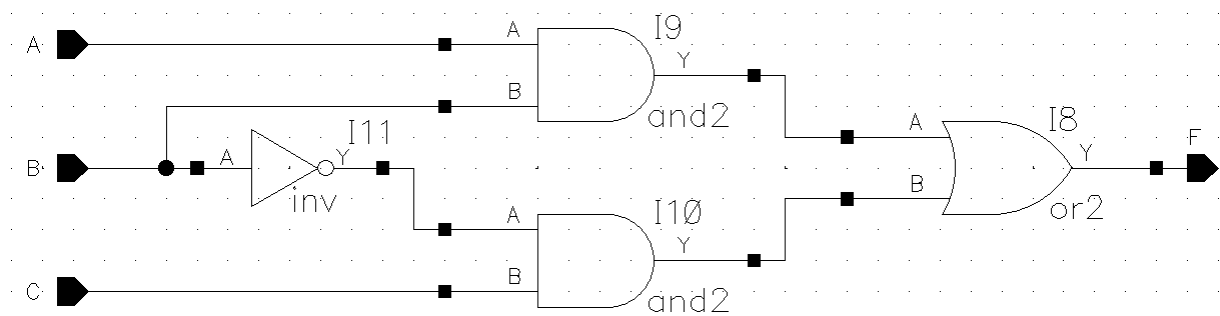
b.) Assign  $F = (A \& B) \mid (C \& D \& \sim E) \mid (\sim A \& E)$

c.)  $F = \overline{\overline{\overline{\overline{\overline{\overline{A} + \overline{B} + \overline{C} + \overline{D} + \overline{E} + A + E}}}}}$



**Problem 10:**

a)  $F = AB + \bar{B}C$



b)  $F = \overline{\overline{A}B} * (B + \overline{C})$

