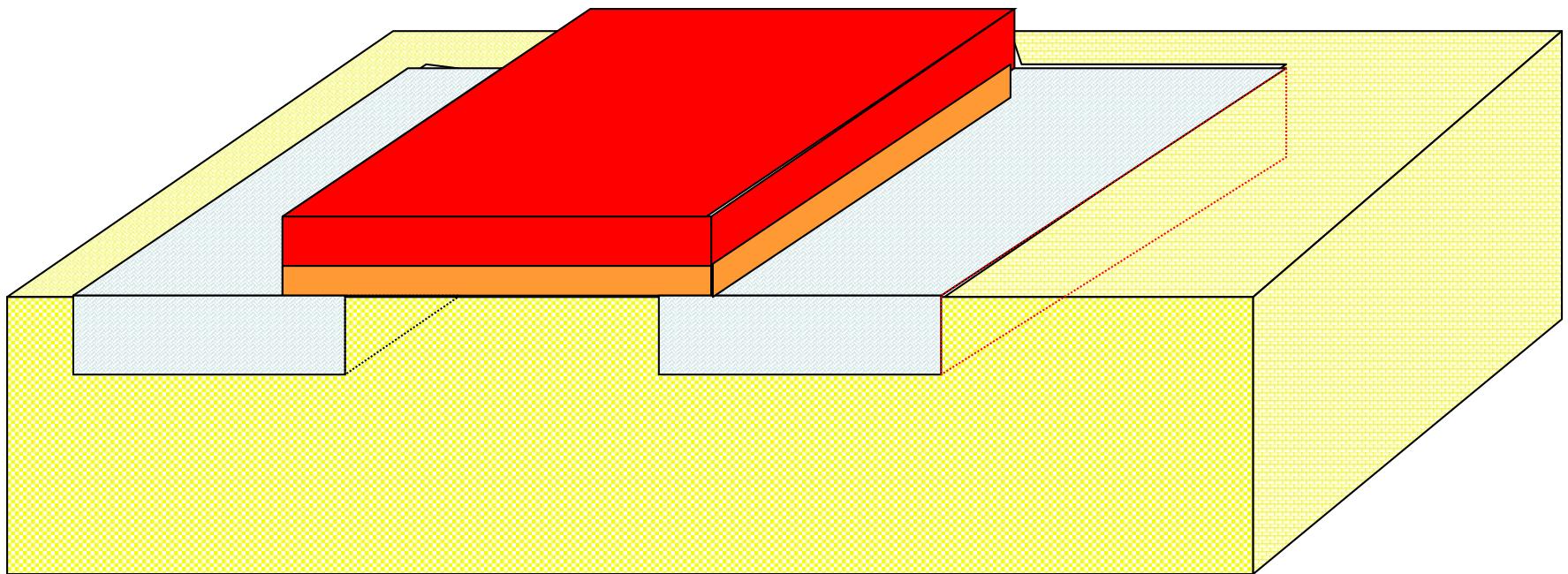


# EE 330

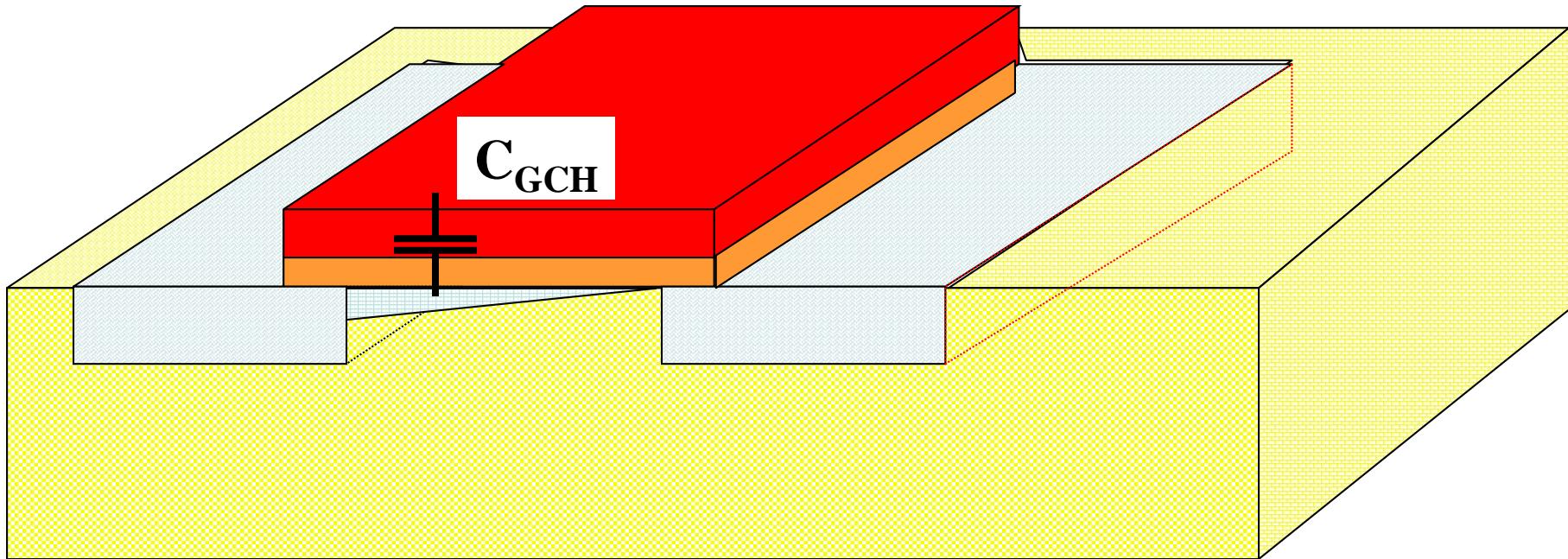
## Lecture 35

- Parasitic Capacitances in MOS Devices
- Digital Systems

# Parasitic Capacitors in MOSFET

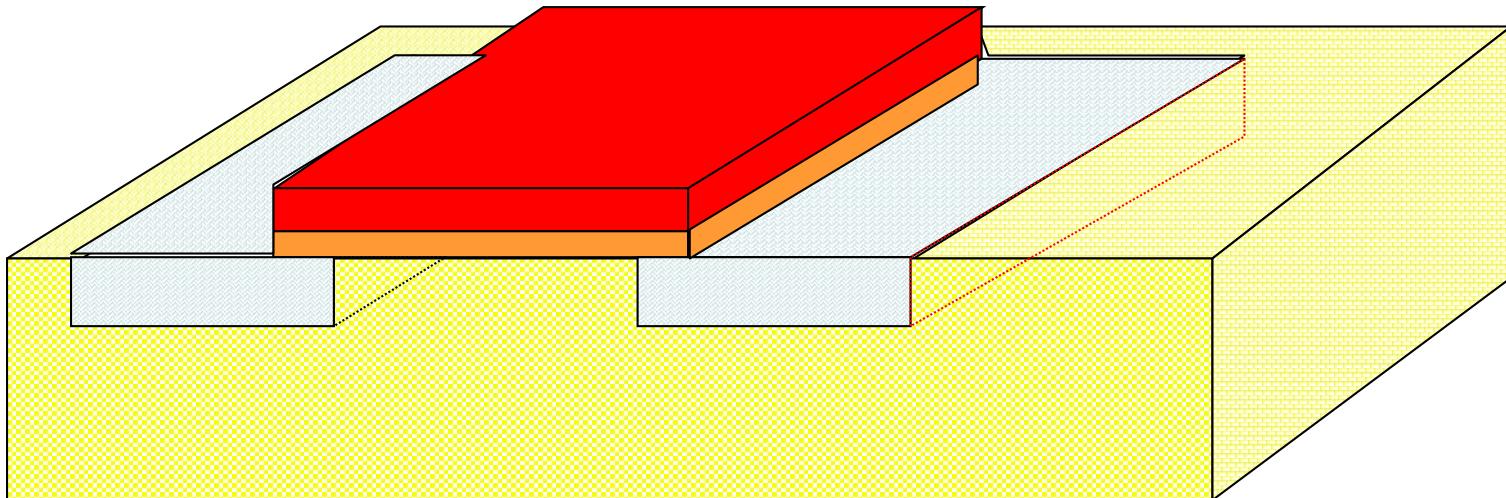


# Parasitic Capacitors in MOSFET

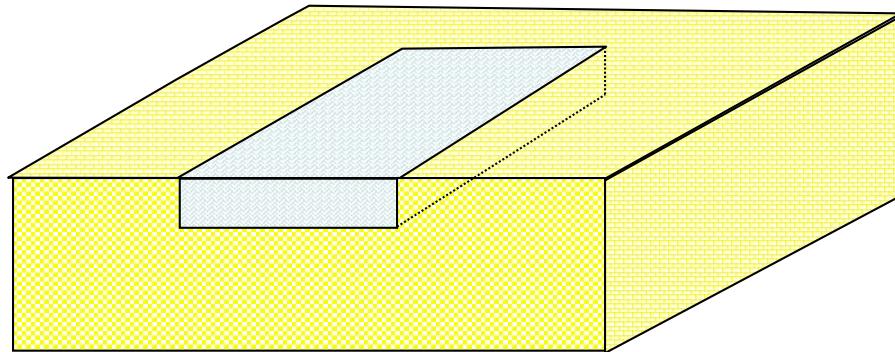


- This capacitance was modeled previously and exists when the transistor is operating in triode or saturation
- But there are others that also affect high-frequency or high-speed operation

# Parasitic Capacitors in MOSFET

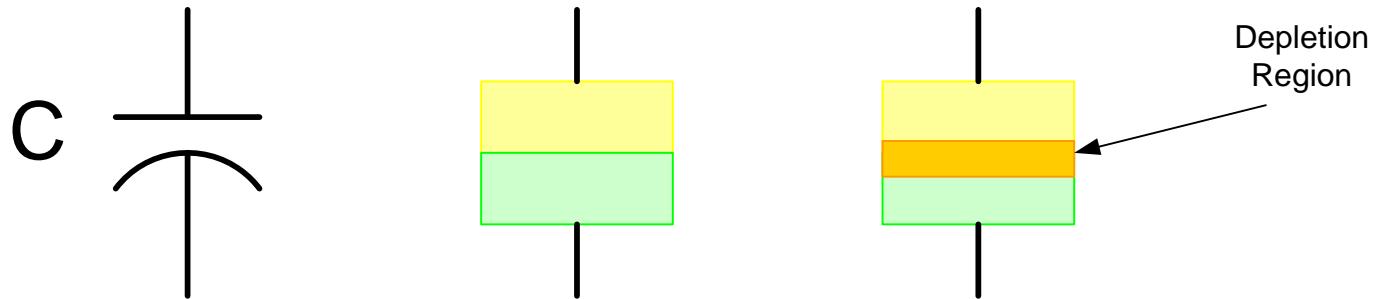
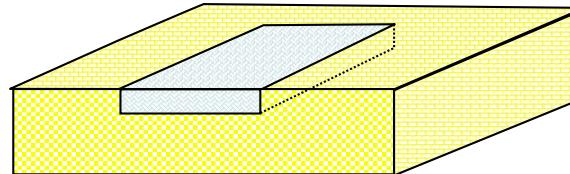


Recall that pn junctions have a depletion region!

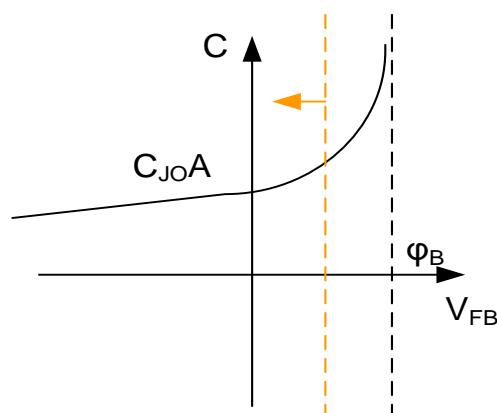


# Parasitic Capacitors in MOSFET

pn junction capacitance



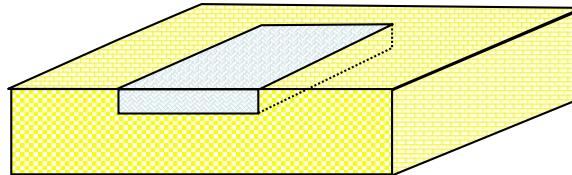
For  $V_{FB} < \phi_B/2$



$$C = \frac{C_{JOA}}{\left(1 - \frac{V_{FB}}{\phi_B}\right)^m}$$

# Parasitic Capacitors in MOSFET

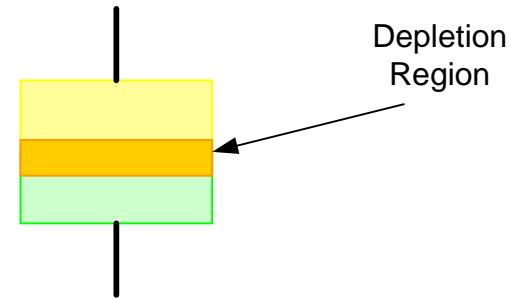
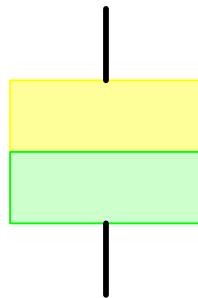
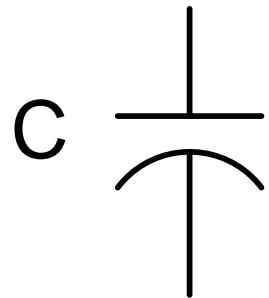
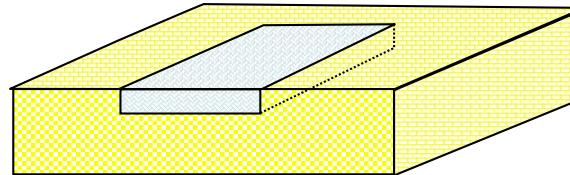
pn junction capacitance



The bottom and the sidewall:

# Parasitic Capacitors in MOSFET

pn junction capacitance



For a pn junction capacitor

$$C_J = C_{BOT} A + C_{SW} P$$

$$C_{BOT} = \frac{C_{BOT} A}{\left(1 - \frac{V_{FB}}{\Phi_B}\right)^m}$$

$$C_{SW} = \frac{C_{SW} P}{\left(1 - \frac{V_{FB}}{\Phi_B}\right)^m}$$

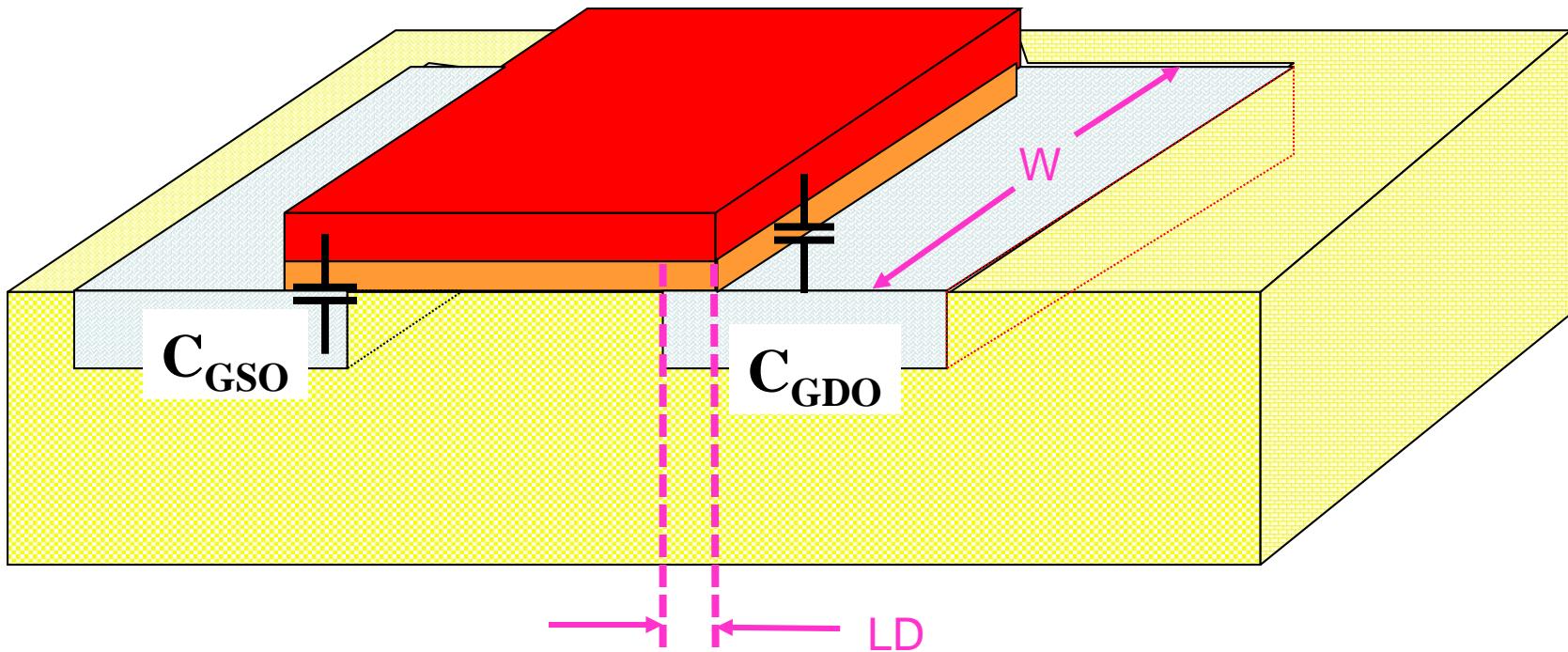
# Types of Capacitors in MOSFETs

1. Fixed Capacitors
  - a. Fixed Geometry
  - b. Junction
2. Operating Region Dependent



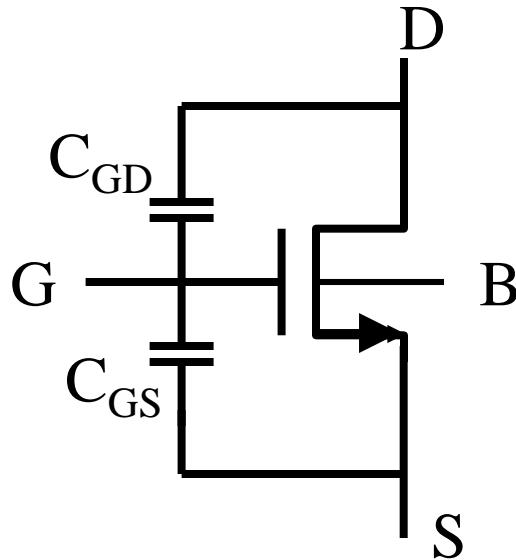
# Parasitic Capacitors in MOSFET

## Fixed Capacitors – Fixed Geometry



Overlap Capacitors:  $C_{GDO}, C_{GSO}$

# Parasitic Capacitance Summary



	Cutoff	Ohmic	Saturation
C <sub>GS</sub>	CoxWL <sub>D</sub>	CoxWL <sub>D</sub>	CoxWL <sub>D</sub>
C <sub>GD</sub>	CoxWL <sub>D</sub>	CoxWL <sub>D</sub>	CoxWL <sub>D</sub>

L<sub>D</sub> is a model parameter

# Overlap Capacitance Model Parameters

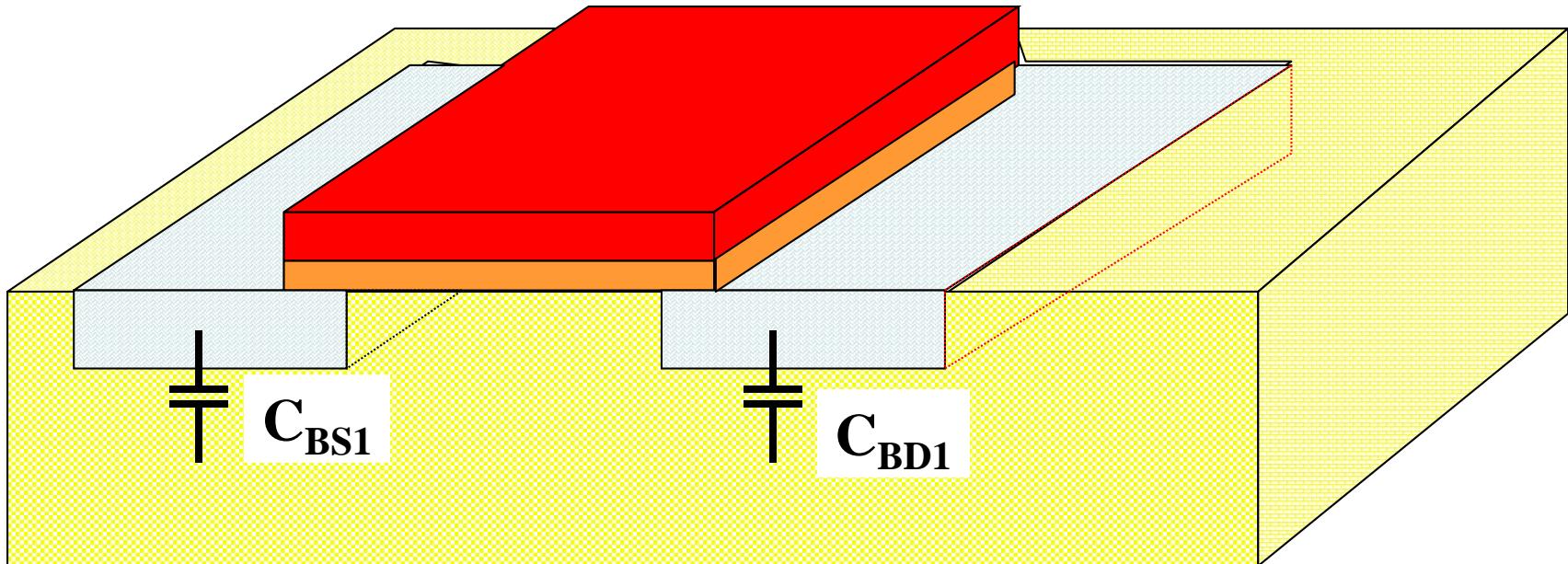
# Types of Capacitors in MOSFETs

1. Fixed Capacitors
  - a. Fixed Geometry
  - b. Junction
2. Operating Region Dependent



# Parasitic Capacitors in MOSFET

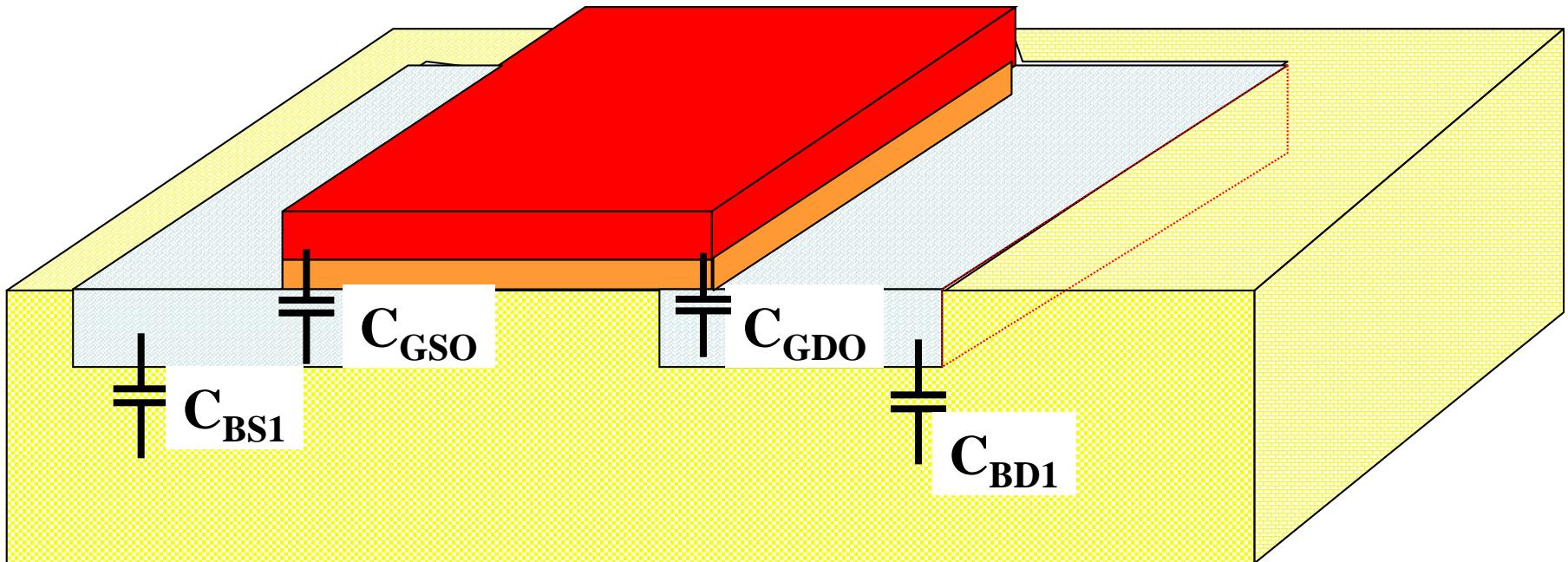
## Fixed Capacitors- Junction



Junction Capacitors:  $C_{BS1}$ ,  $C_{BD1}$

# Parasitic Capacitors in MOSFET

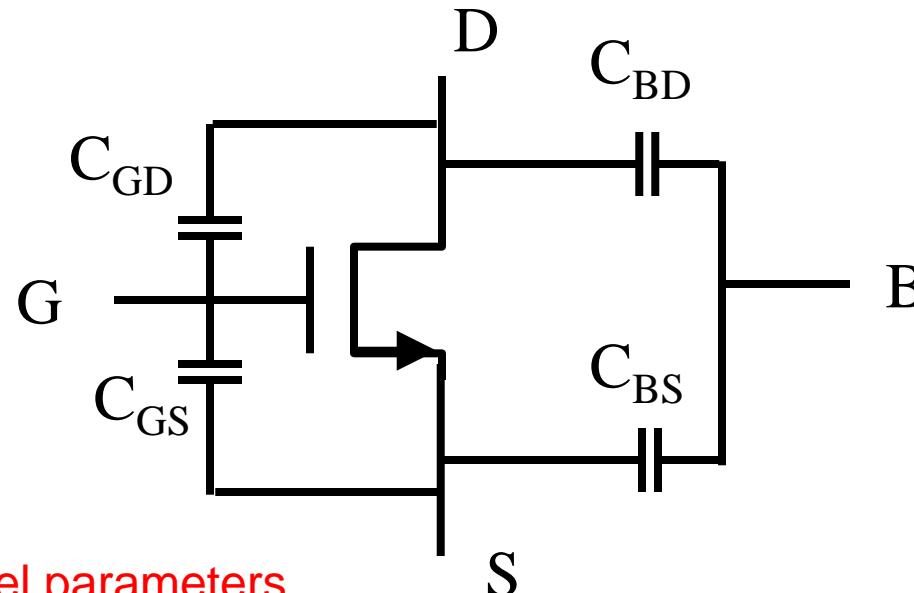
## Fixed Capacitors



Overlap Capacitors:  $C_{GDO}, C_{GSO}$

Junction Capacitors:  $C_{BS1}, C_{BD1}$

# Fixed Parasitic Capacitance Summary



$C_{BOT}$  and  $C_{SW}$  are model parameters

	<b>Cutoff</b>	<b>Ohmic</b>	<b>Saturation</b>
$C_{GS}$	$CoxWL_D$	$CoxWL_D$	$CoxWL_D$
$C_{GD}$	$CoxWL_D$	$CoxWL_D$	$CoxWL_D$
$C_{BG}$			
$C_{BS}$	$C_{BS1} = C_{BOT}A_S + C_{SW}P_S$	$C_{BS1} = C_{BOT}A_S + C_{SW}P_S$	$C_{BS1} = C_{BOT}A_S + C_{SW}P_S$
$C_{BD}$	$C_{BD1} = C_{BOT}A_D + C_{SW}P_D$	$C_{BD1} = C_{BOT}A_D + C_{SW}P_D$	$C_{BD1} = C_{BOT}A_D + C_{SW}P_D$

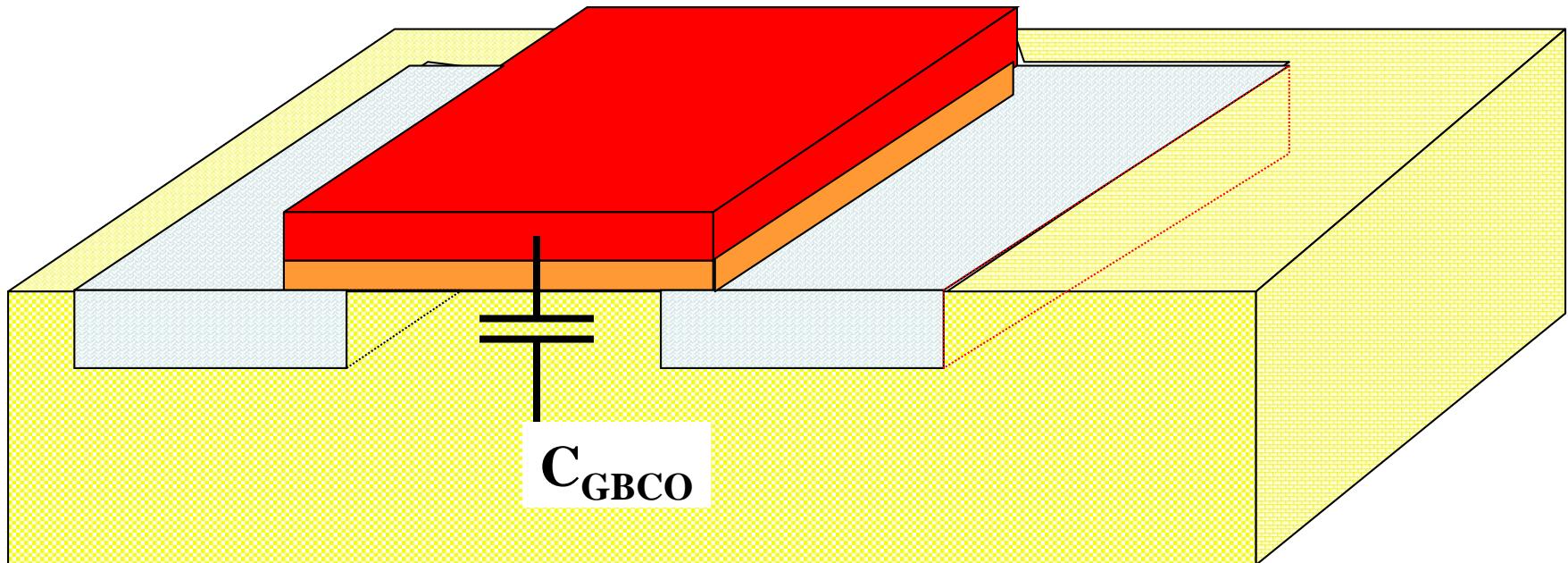
# $C_{BOT}$ and $C_{SW}$ model parameters

# Types of Capacitors in MOSFETs

1. Fixed Capacitors
  - a. Fixed Geometry
  - b. Junction
2. Operating Region Dependent

# Parasitic Capacitors in MOSFET

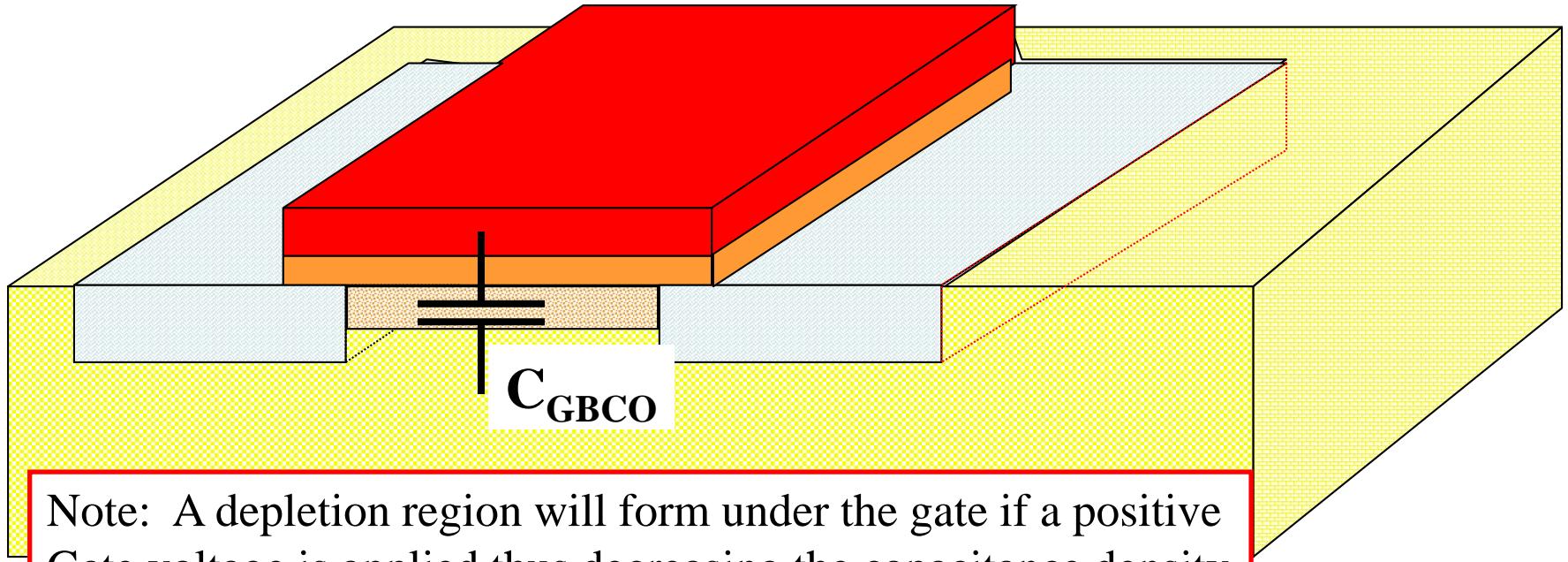
## Operation Region Dependent -- Cutoff



Cutoff Capacitor:  $C_{GBCO}$

# Parasitic Capacitors in MOSFET

## Operation Region Dependent -- Cutoff

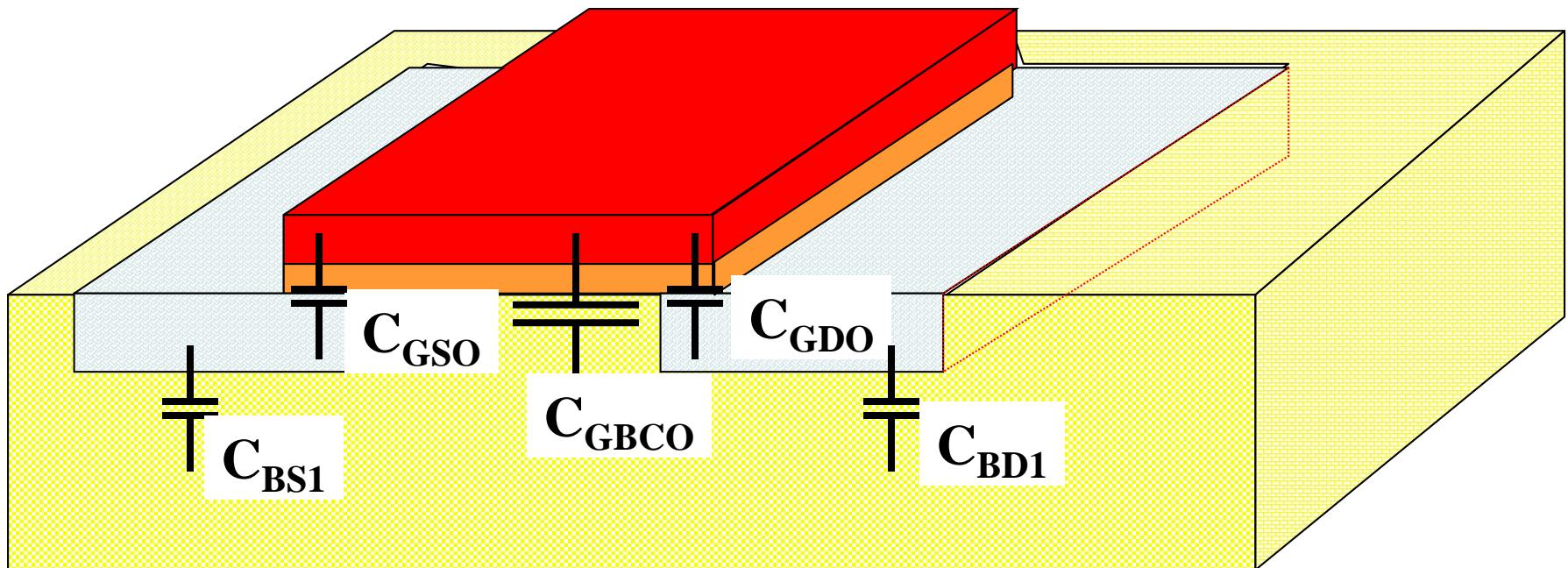


Note: A depletion region will form under the gate if a positive Gate voltage is applied thus decreasing the capacitance density

**Cutoff Capacitor:  $C_{GBCO}$**

# Parasitic Capacitors in MOSFET

## Operation Region Dependent and Fixed -- Cutoff

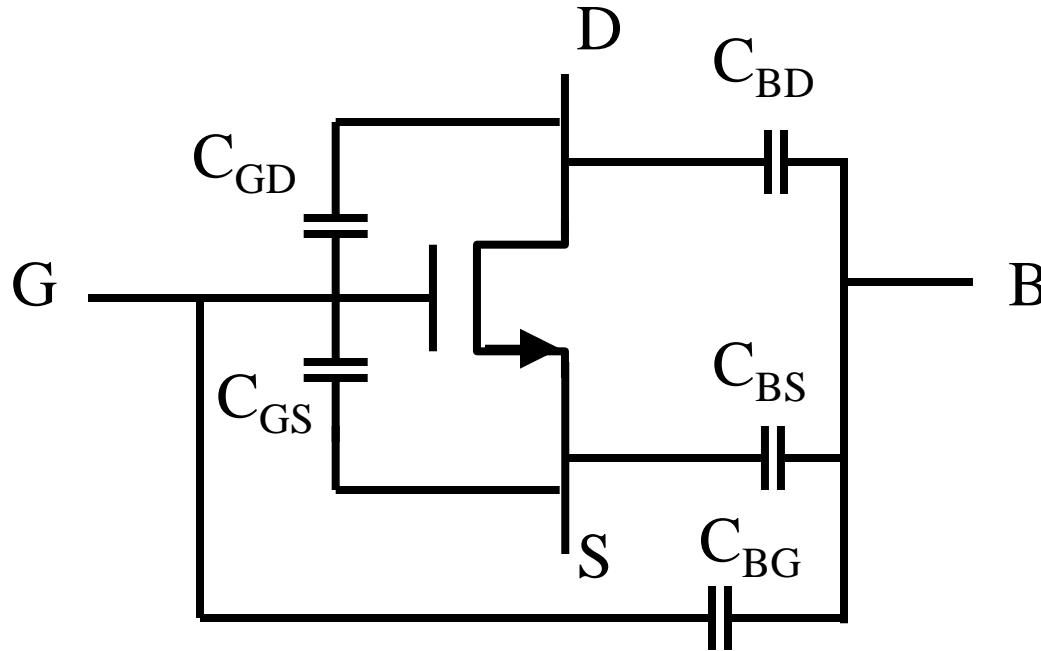


Overlap Capacitors:  $C_{GDO}, C_{GSO}$

Junction Capacitors:  $C_{BS1}, C_{BD1}$

**Cutoff Capacitor:**  $C_{GBCO}$

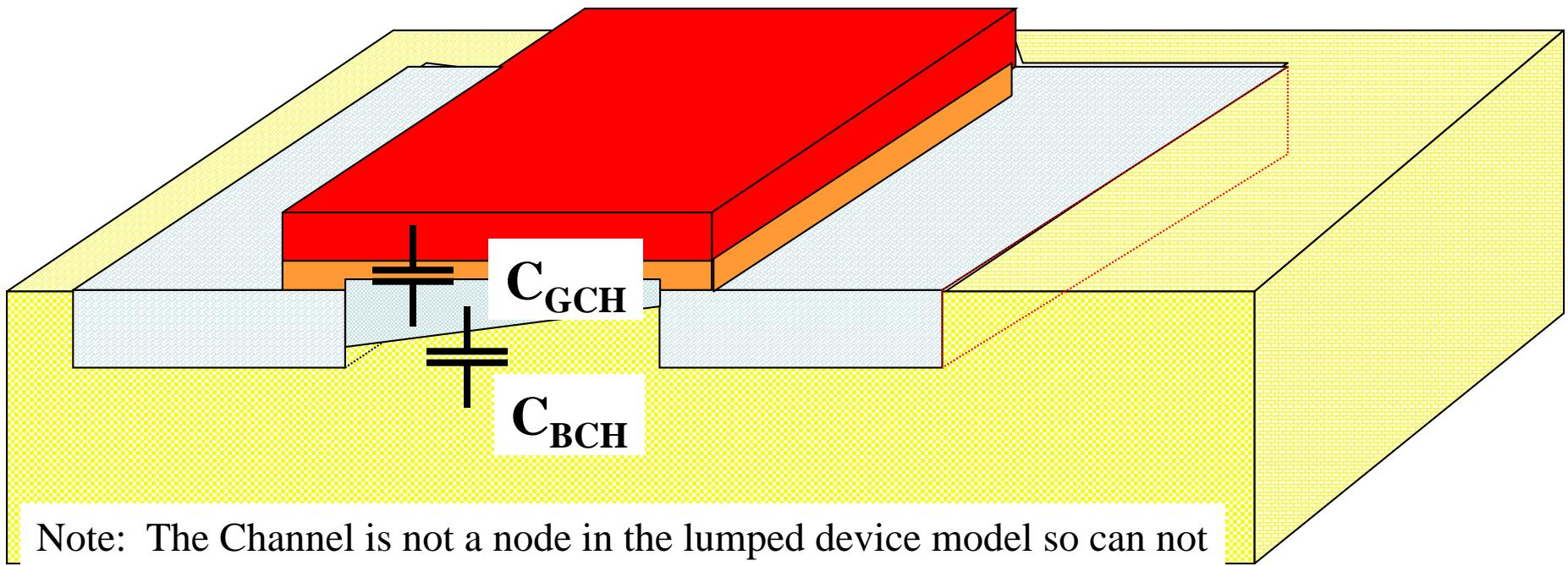
# Parasitic Capacitance Summary



	Cutoff	Ohmic	Saturation
$C_{GS}$	$C_{oxWL_D}$		
$C_{GD}$	$C_{oxWL_D}$		
$C_{BG}$	$C_{oxWL}$ (or less)		
$C_{BS}$	$C_{BOT}A_S + C_{SW}P_S$		
$C_{BD}$	$C_{BOT}A_D + C_{SW}P_D$		

# Parasitic Capacitors in MOSFET

## Operation Region Dependent -- Ohmic



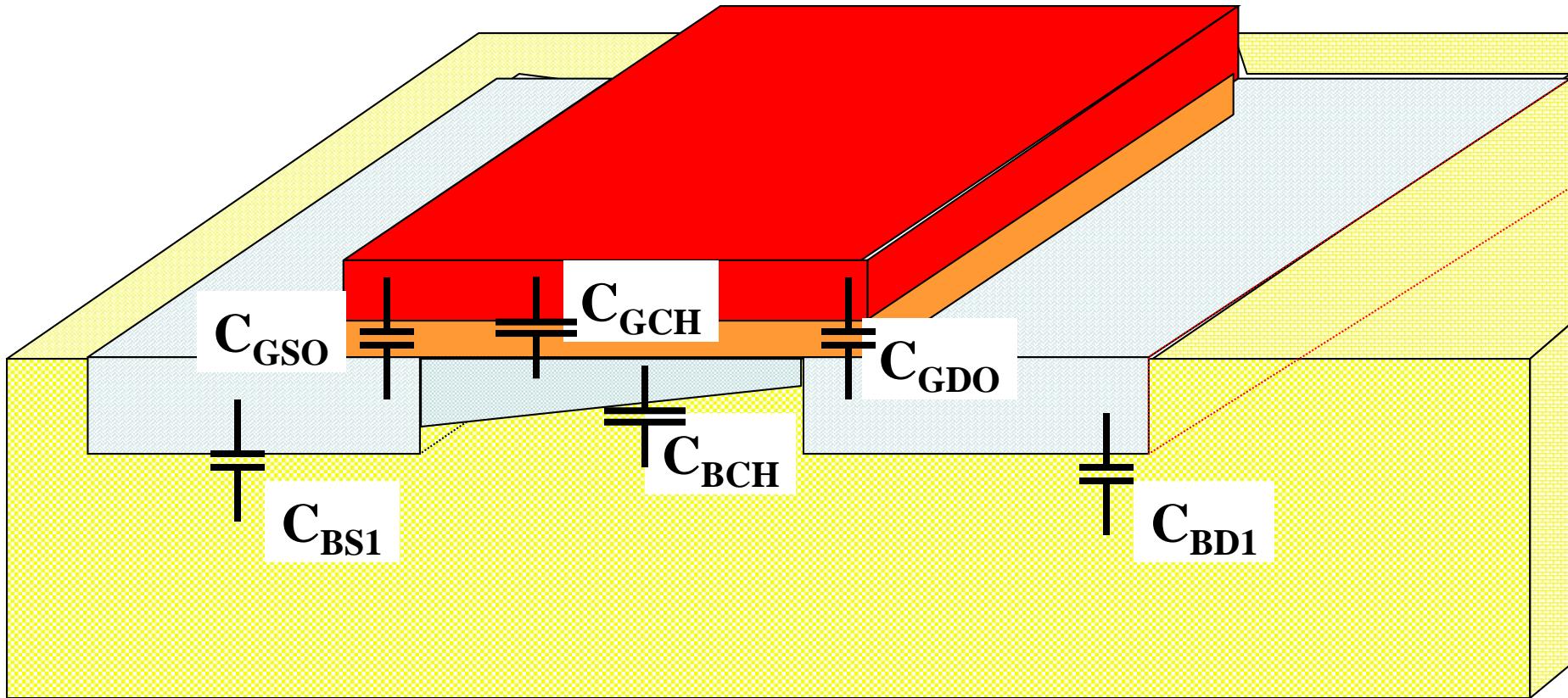
Note: The Channel is not a node in the lumped device model so can not directly include this distributed capacitance in existing models

Note: The distributed channel capacitance is usually lumped and split evenly between the source and drain nodes

**Ohmic Capacitor:  $C_{GCH}$ ,  $C_{BCH}$**

# Parasitic Capacitors in MOSFET

## Operation Region Dependent and Fixed -- Ohmic

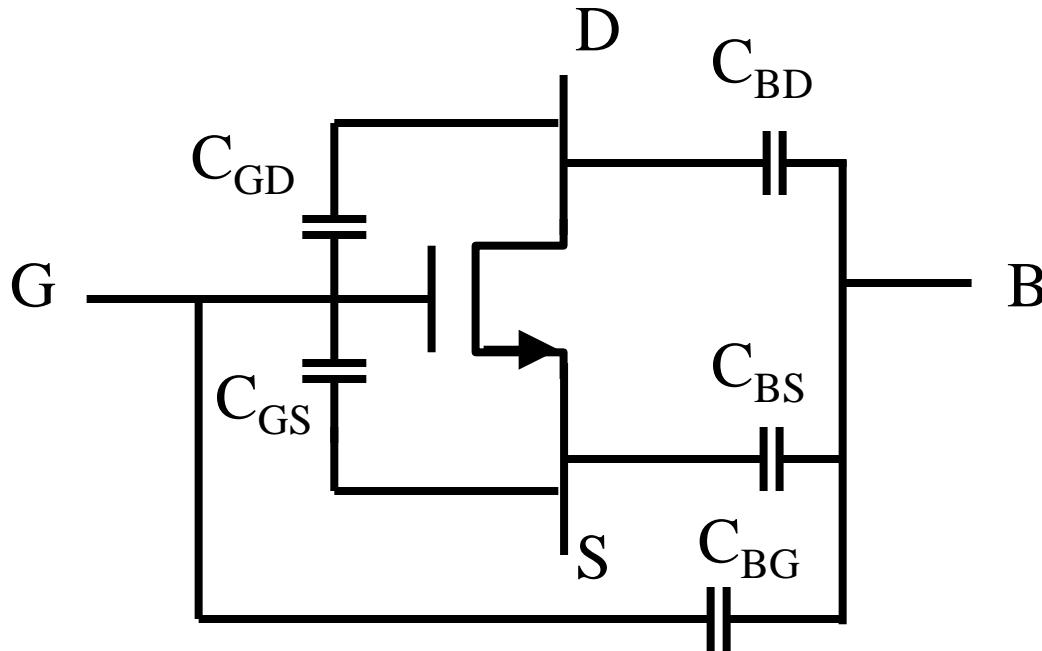


Overlap Capacitors:  $C_{GDO}, C_{GSO}$

Junction Capacitors:  $C_{BS1}, C_{BD1}$

**Ohmic Capacitor:**  $C_{GCH}, C_{BCH}$

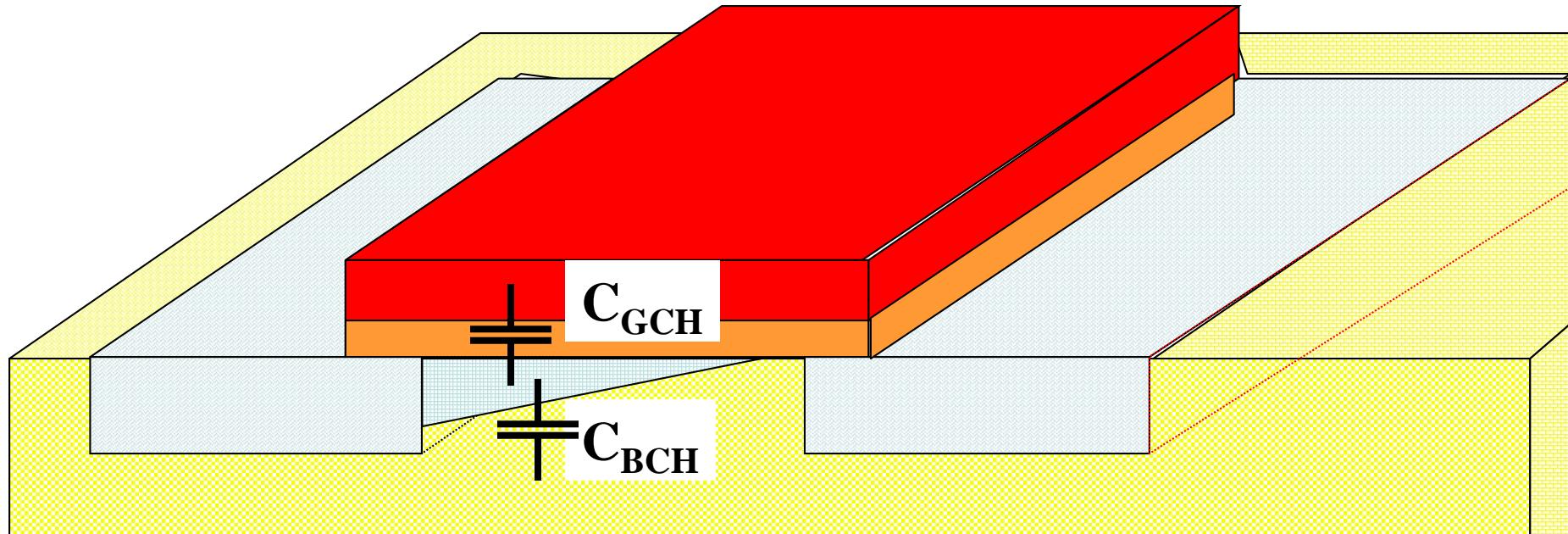
# Parasitic Capacitance Summary



	<b>Cutoff</b>	<b>Ohmic</b>	<b>Saturation</b>
$C_{GS}$	$C_{oxWL_D}$	$C_{oxWL_D}$	
$C_{GD}$	$C_{oxWL_D}$	$C_{oxWL_D}$	
$C_{BG}$	$C_{oxWL}$ (or less)	0	
$C_{BS}$	$C_{BOT}A_S + C_{SW}P_S$	$C_{BS1} = C_{BOT}A_S + C_{SW}P_S$	
$C_{BD}$	$C_{BOT}A_D + C_{SW}P_D$	$C_{BD1} = C_{BOT}A_D + C_{SW}P_D$	

# Parasitic Capacitors in MOSFET

## Operation Region Dependent -- Saturation

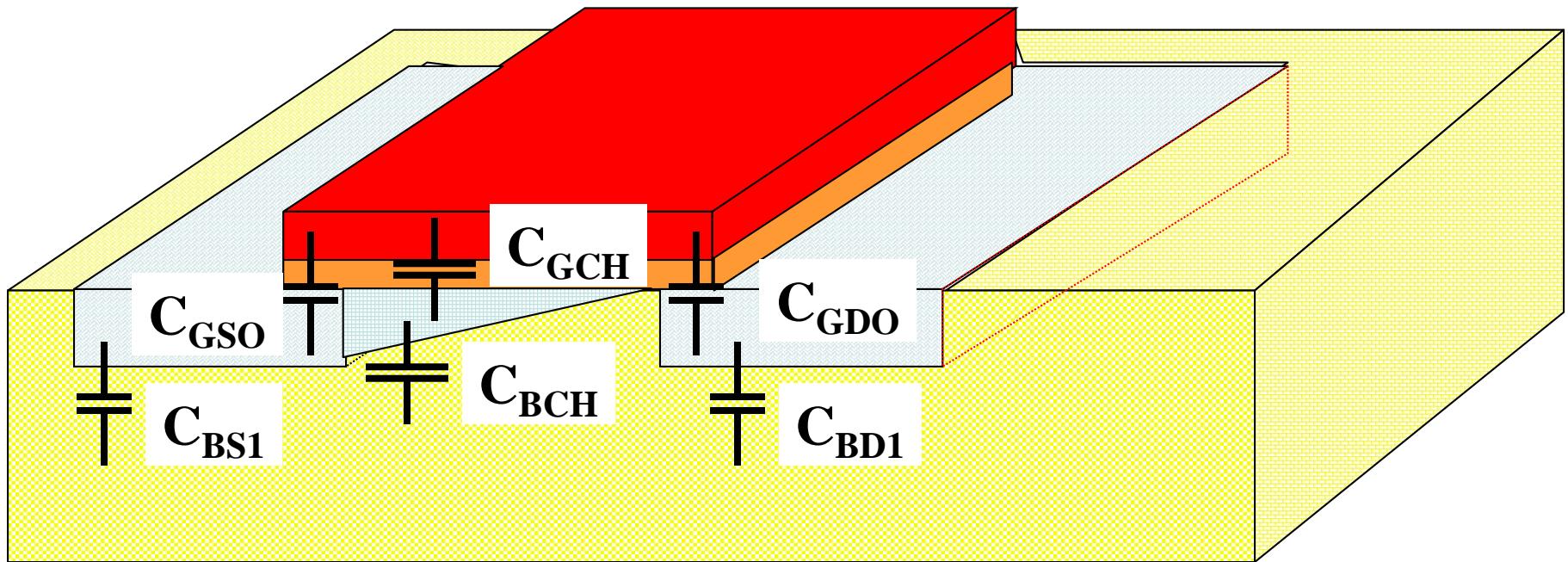


Note: Since the channel is an extension of the source when in saturation, the distributed capacitors to the channel are generally lumped to the source node

**Saturation Capacitors:  $C_{GCH}$ ,  $C_{BCH}$**

# Parasitic Capacitors in MOSFET

Operation Region Dependent and Fixed --Saturation



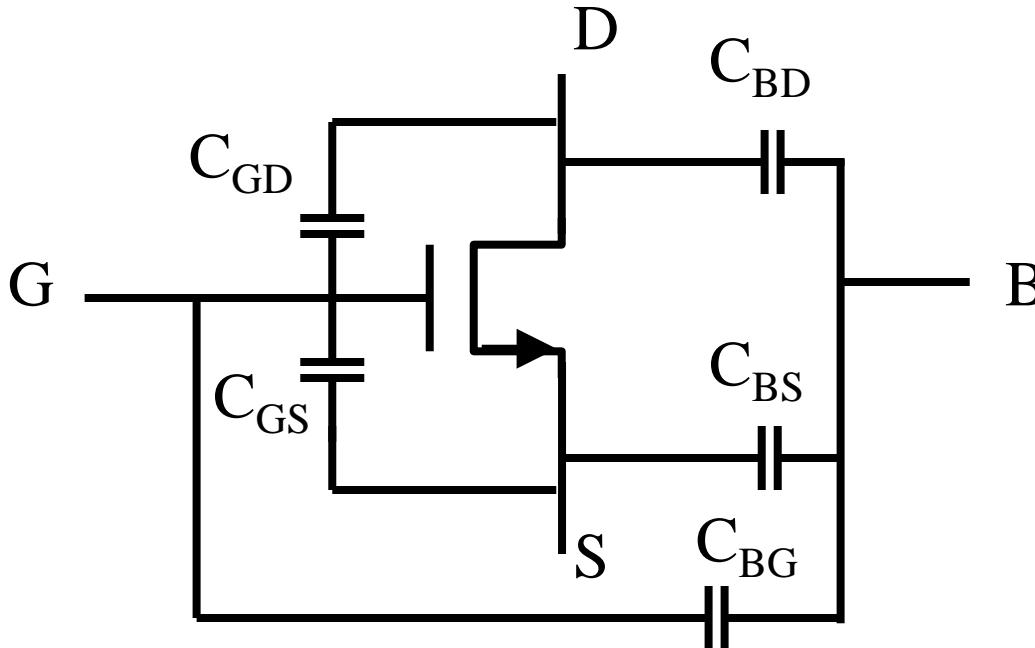
Overlap Capacitors:  $C_{GDO}, C_{GSO}$

Junction Capacitors:  $C_{BS1}, C_{BD1}$

**Saturation Capacitors:**  $C_{GCH}, C_{BCH}$

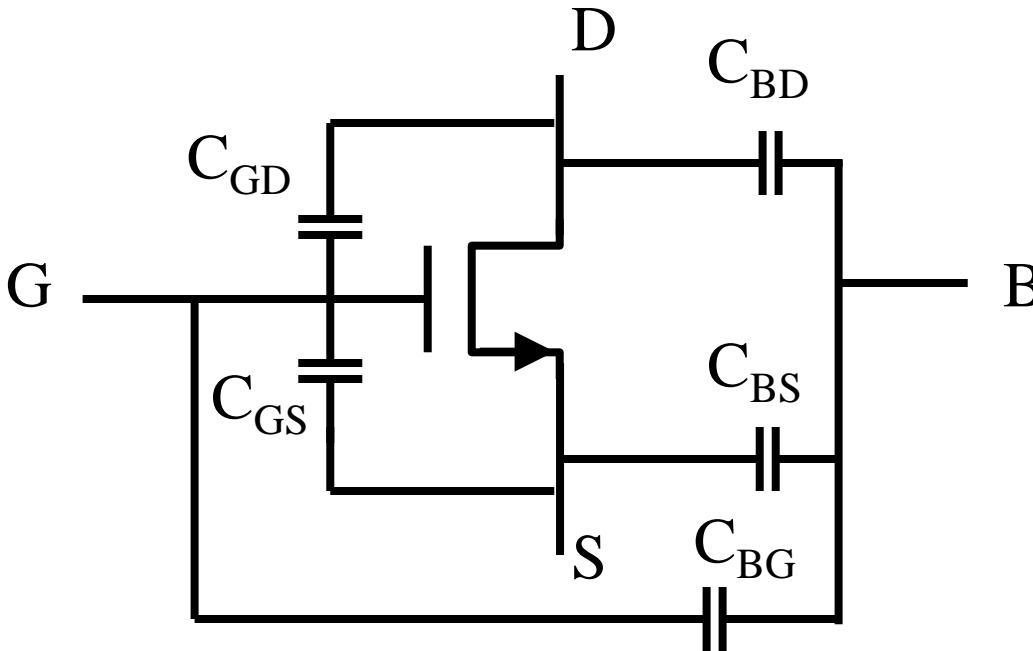
- $2/3 C_{Ox}WL$  is often attributed to  $C_{GCH}$  to account for LD and saturation
- This approximation is reasonable for minimum-length devices but not so good for longer devices

# Parasitic Capacitance Summary



	Cutoff	Ohmic	Saturation
$C_{GS}$	$C_{ox}WL_D$	$C_{ox}WL_D + 0.5C_{ox}WL$	$C_{ox}WL_D + (2/3)C_{ox}WL$
$C_{GD}$	$C_{ox}WL_D$	$C_{ox}WL_D + 0.5C_{ox}WL$	$C_{ox}WL_D$
$C_{BG}$	$C_{ox}WL$ (or less)	0	0
$C_{BS}$	$C_{BOT}A_S + C_{SW}P_S$	$C_{BOT}A_S + C_{SW}P_S + 0.5WLC_{BOTCH}$	$C_{BOT}A_S + C_{SW}P_S + (2/3)WLC_{BOTCH}$
$C_{BD}$	$C_{BOT}A_D + C_{SW}P_D$	$C_{BOT}A_D + C_{SW}P_D + 0.5WLC_{BOTCH}$	$C_{BOT}A_D + C_{SW}P_D$

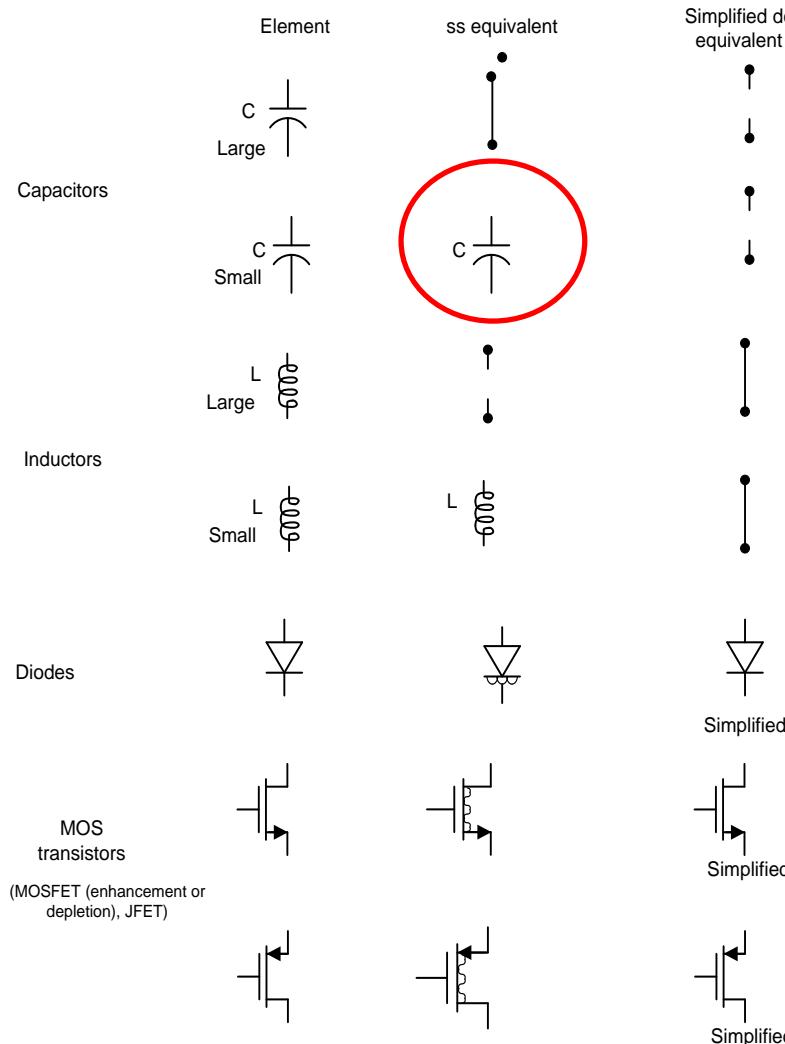
# Parasitic Capacitance Summary



	<b>Cutoff</b>	<b>Ohmic</b>	<b>Saturation</b>
$C_{GS}$	$C_{ox}WL_D$	$C_{ox}WL_D + 0.5C_{ox}WL$	$C_{ox}WL_D + (2/3)C_{ox}WL$
$C_{GD}$	$C_{ox}WL_D$	$C_{ox}WL_D + 0.5C_{ox}WL$	$C_{ox}WL_D$
$C_{BG}$	$C_{ox}WL$ (or less)	0	0
$C_{BS}$	$C_{BOT}A_S + C_{SW}P_S$	$C_{BOT}A_S + C_{SW}P_S + 0.5WLC_{BOTCH}$	$C_{BOT}A_S + C_{SW}P_S + (2/3)WLC_{BOTCH}$
$C_{BD}$	$C_{BOT}A_D + C_{SW}P_D$	$C_{BOT}A_D + C_{SW}P_D + 0.5WLC_{BOTCH}$	$C_{BOT}A_D + C_{SW}P_D$

# Recall:

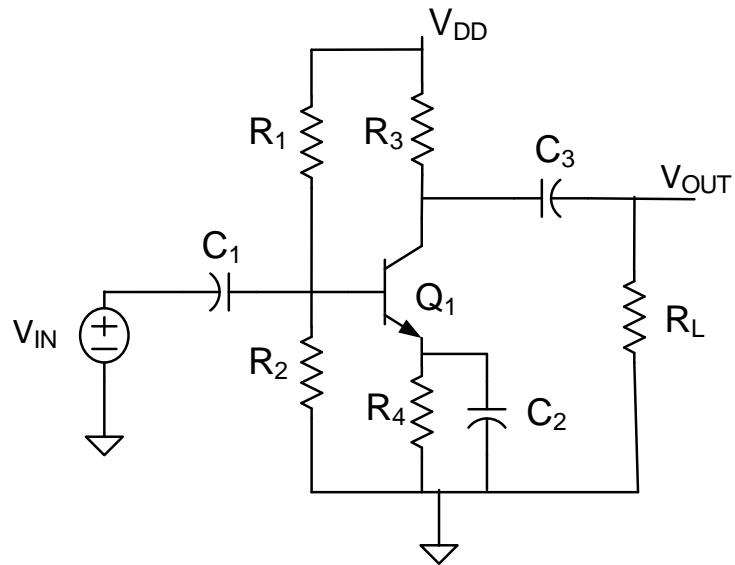
## Small-signal and simplified dc equivalent elements



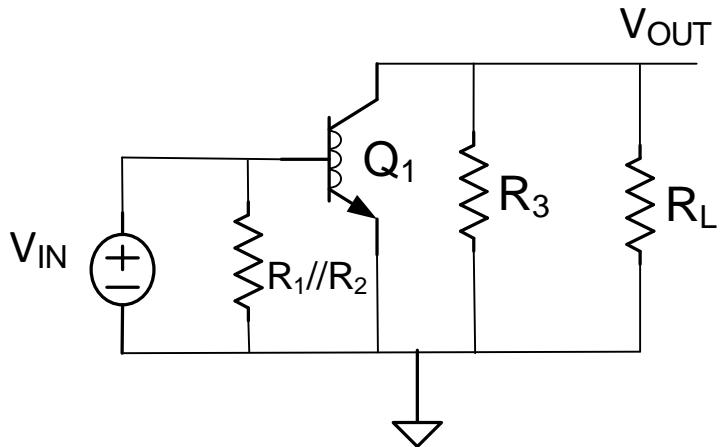
Have not yet considered situations where the small capacitor is relevant in small-signal analysis

# Amplifiers with Small Capacitors

Recall:



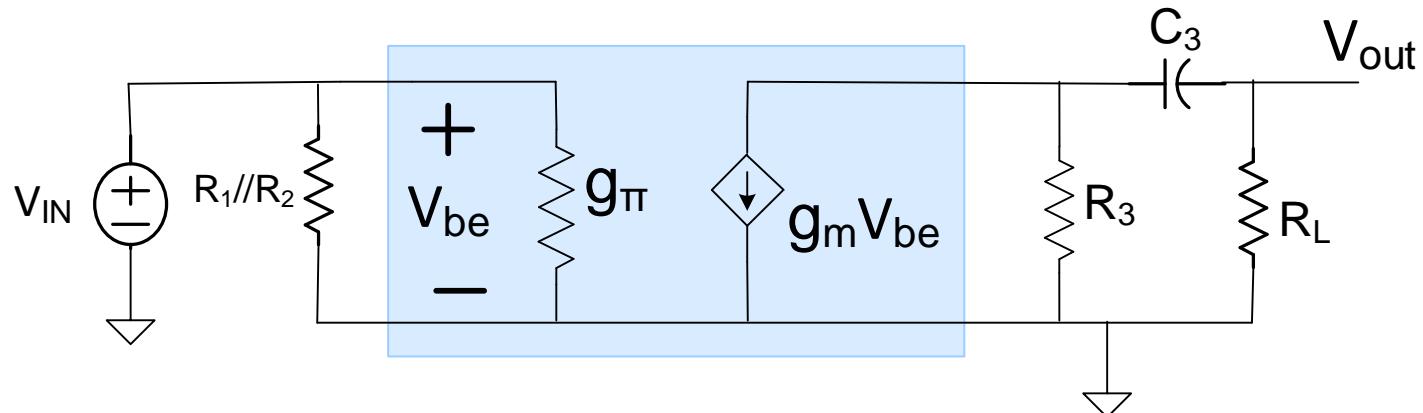
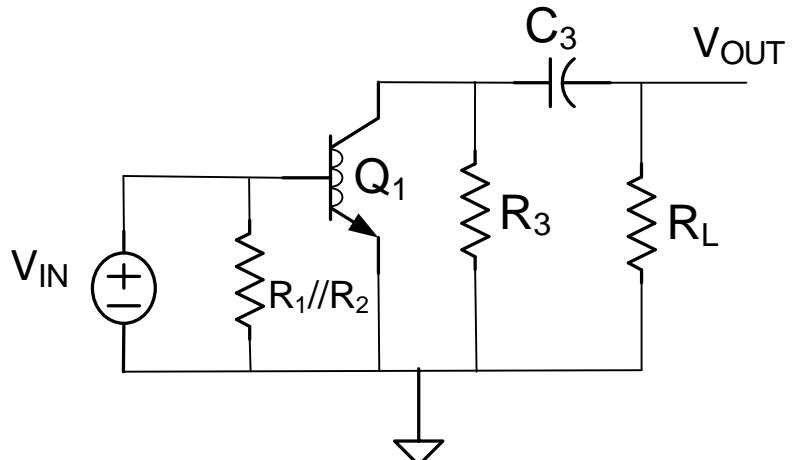
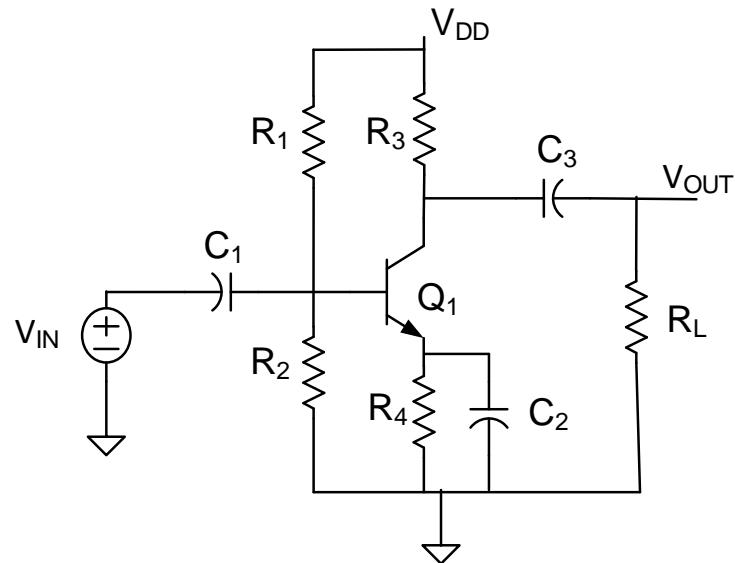
If capacitors are large



$$A_V = -g_{m1} \bullet R_3 // R_L$$

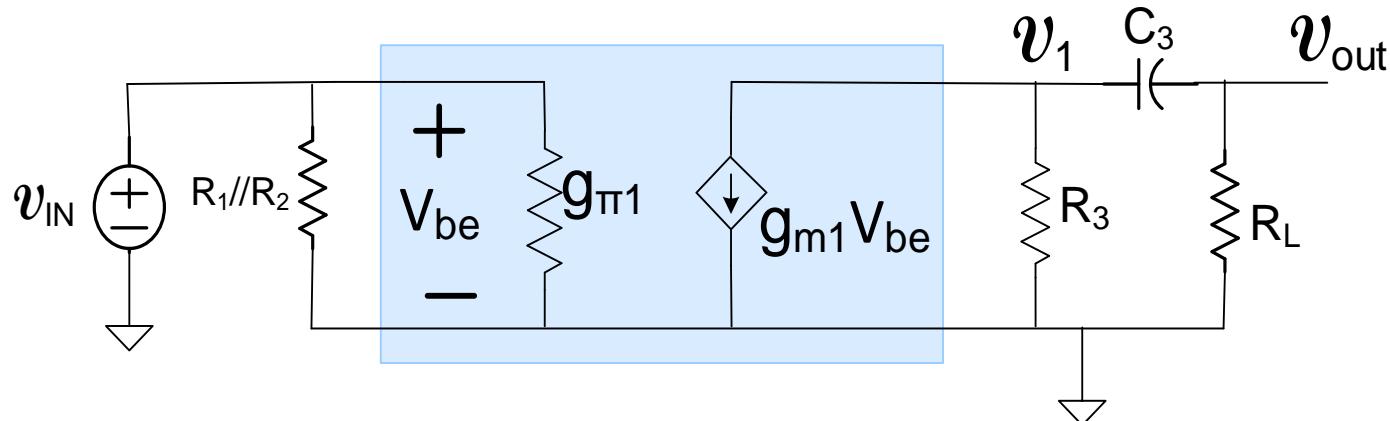
# Amplifiers with Small Capacitors

What if  $C_1$  and  $C_2$  large but  $C_3$  not large?:



# Amplifiers with Small Capacitors

What if  $C_1$  and  $C_2$  large but  $C_3$  not large?:



From KCL:

$$\left. \begin{aligned} v_{OUT}(sC_3 + G_L) &= v_s C_3 \\ v_i(sC_3 + G_3) + g_{m1}v_{IN} &= v_{OUT}sC_3 \end{aligned} \right\}$$

Serves as a first-order high-pass filter

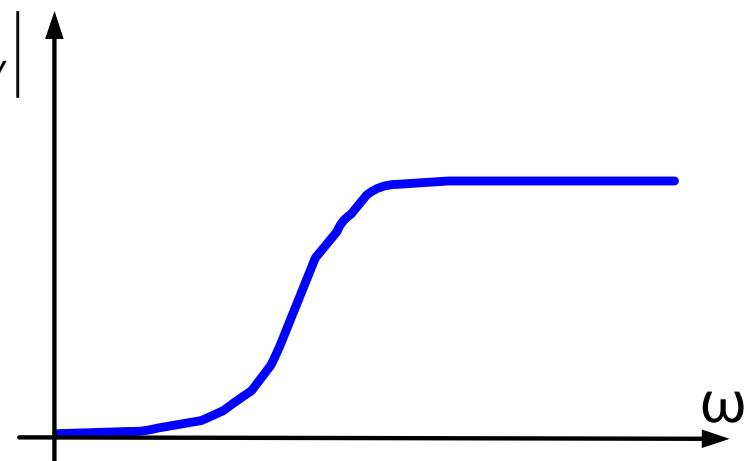
$$|A_v|$$

Solving:

$$\frac{v_{OUT}}{v_{IN}} = -\frac{-sC_3 g_{m1}}{sC_3(G_L + G_3) + G_3 G_L}$$

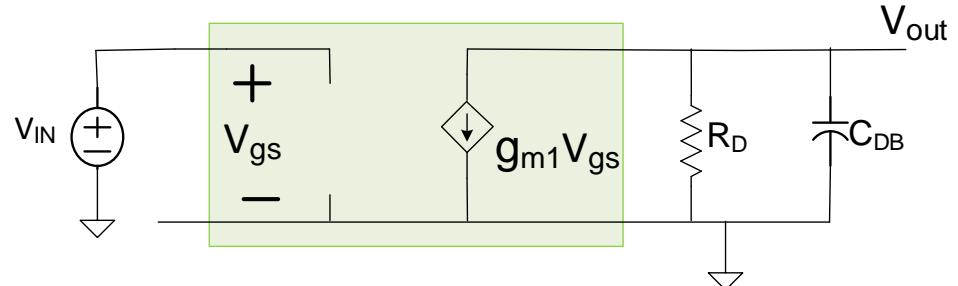
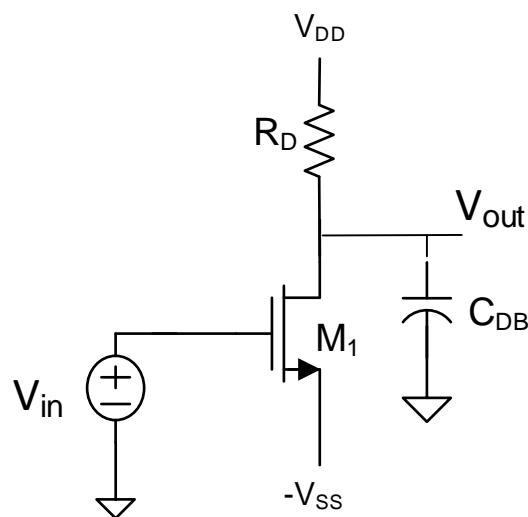
Equivalently:

$$\frac{v_{OUT}}{v_{IN}} = -\frac{g_{m1} sC_3 R_3 R_L}{sC_3(R_L + R_3) + 1}$$



# Amplifiers with Small Capacitors

Consider parasitic  $C_{DB}$



By KCL:

$$v_{OUT} (sC_{DB} + G_D) = -g_{m1} v_{IN}$$

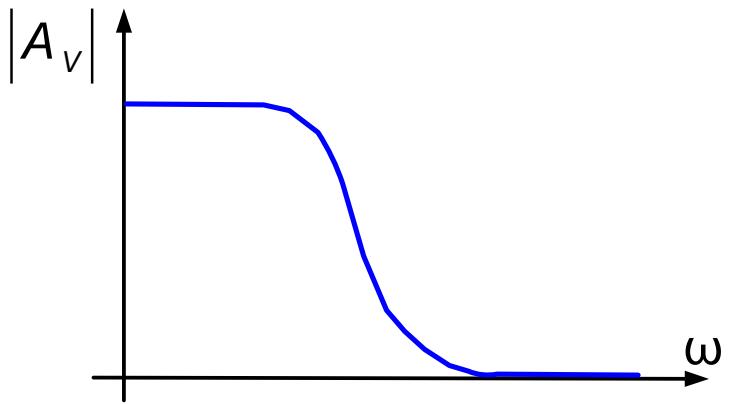
Causes gain to decrease at high frequencies

Solving:

$$\frac{v_{OUT}}{v_{IN}} = -\frac{-g_{m1}}{sC_{DB} + G_D}$$

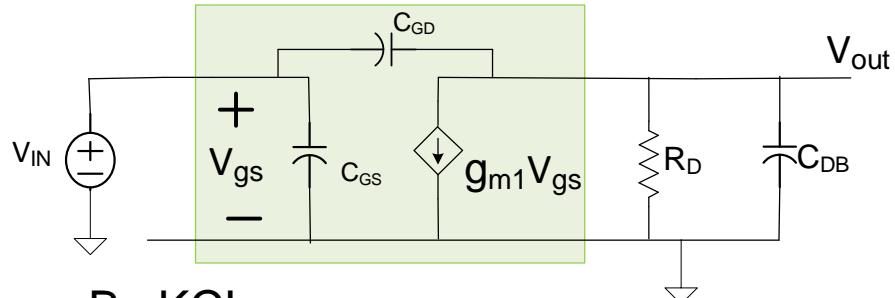
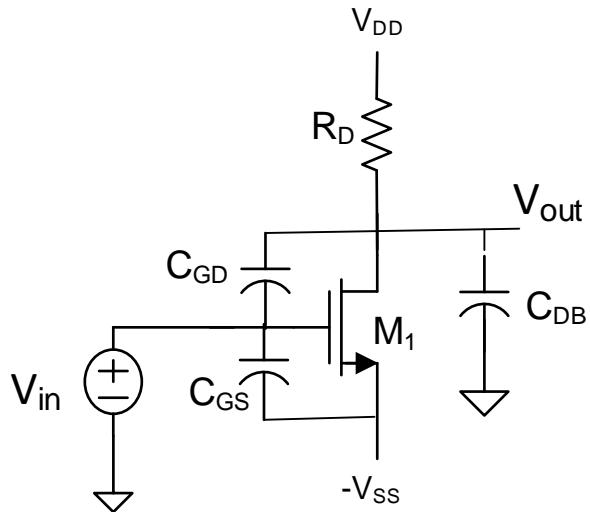
Equivalently:

$$\frac{v_{OUT}}{v_{IN}} = -\frac{-g_{m1}R_D}{sC_{DB}R_D + 1}$$



# Amplifiers with Small Capacitors

Consider parasitic  $C_{GS}$ ,  $C_{GD}$ , and  $C_{DB}$



By KCL:

$$v_{out} (s[C_{DB} + C_{GD}] + G_D) = -g_{m1} v_{IN} + sC_{GD} v_{IN}$$

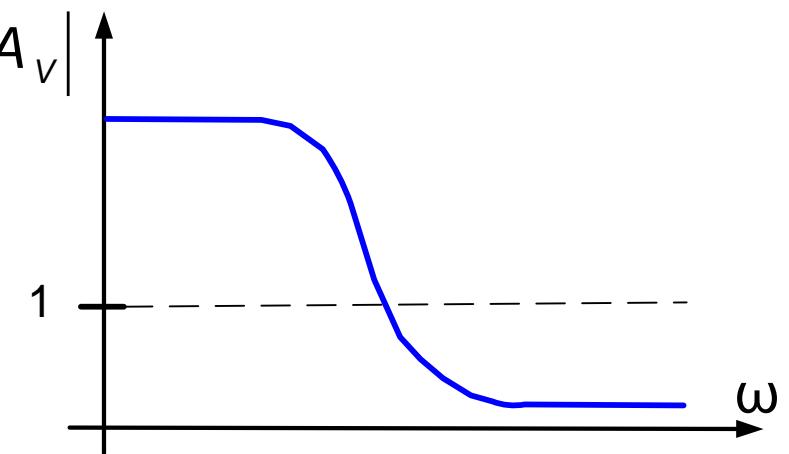
Causes gain to decrease at high frequencies  
Has one LHP pole and one RHP zero

Solving:

$$\frac{v_{out}}{v_{IN}} = -\frac{-g_{m1} + sC_{GD}}{s[C_{DB} + C_{GD}] + G_D}$$

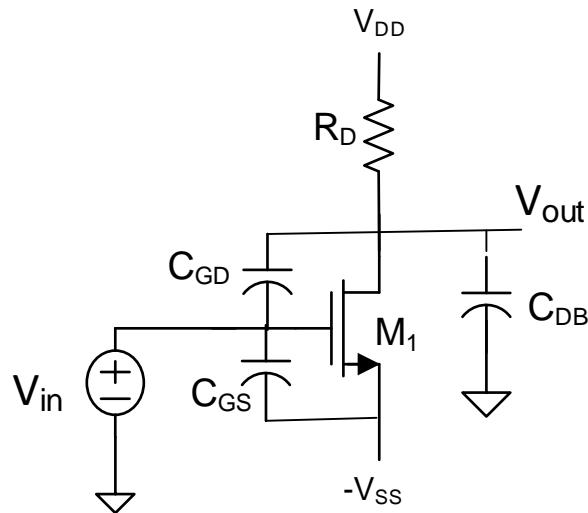
Equivalently:

$$\frac{v_{out}}{v_{IN}} = -\frac{-R_D(g_{m1} - sC_{GD})}{s[C_{DB} + C_{GD}]R_D + 1}$$



# Amplifiers with Small Capacitors

Consider parasitic  $C_{GS}$ ,  $C_{GD}$ , and  $C_{DB}$



Device parasitics problematic at high frequencies

$C_{DB}$ ,  $C_{GD}$  and  $C_{GS}$  effects can be significant

Value of parasitic capacitances strongly dependent upon layout

Device parasitics usually not a problem at audio frequencies

Causes gain to decrease at high frequencies:  
has one high frequency LHP pole and one high frequency RHP zero.

# End of Lecture 35